

# A Duality between Forward and Adjoint MPI Communication Routines

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**Abstract** In this article, we explore a natural duality that exist between MPI communication routines in parallel programs, and show the ease of its adjoint implementation via pointers.

**Key words:** ocean modeling, MPI, parallel programming, automatic differentiation, adjoint

## 1. INTRODUCTION

Parallel ocean models are widely used in the oceanographic community as a research tool. Forecasting and estimating the state of the ocean at a particular time is a main staple of ocean modeling. One of the recent major developments in this subject area is the use of the so-called adjoint inverse model, as opposed to the forward simulation that is the usual way to run a model. The adjoint model, which can be derived either manually by hand coding or through automatic differentiation tools such as TAF [1], is a kind of reverse simulation that has proven useful for tracing water flows backwards in time [2], or for measuring sensitivity of specific oceanic variables such as temperature and salinity [3]. Automatic differentiation tools nowadays have few problems adjoining sequential forward codes, however, they still have some ways to go toward adjoining parallel communication routines inside a parallel forward model [4]. We demonstrate that with the right coding structure, parallel communication routines can be adjointed with ease.

## 2. MPI CALLS SETUP

The ocean model that we selected for adjoining is the so-called Modular Ocean Model version 4 (MOM4) [5], originally developed at the Geophysical Fluid Dynamics Laboratory (GFDL) in Princeton university. This model is written in the modern F90 language, with built-in parallel communication routines, written primarily by V. Balaji. The following code snippet illustrates the message exchanges occurring between different CPUs:

```
do m=1,ncpus
if( send_w .AND. domain%list(m)%send_w%overlap )then
is1 = domain%list(m)%send_w%is1; ie1 = domain%list(m)%send_w%ie1
js1 = domain%list(m)%send_w%js1; je1 = domain%list(m)%send_w%je1
...
buffer(pos) = field(is1:ie1,js1:je1)
...
endif
call mpp_send( buffer(pos), plen=msgsize, to_pe=to_pe )
if( recv_e .AND. domain%list(m)%recv_e%overlap )then
is2 = domain%list(m)%recv_e%is2; ie2 = domain%list(m)%recv_e%ie2
js2 = domain%list(m)%recv_e%js2; je2 = domain%list(m)%recv_e%je2
endif
call mpp_recv( buffer(pos), glen=msgsize, from_pe=from_pe )
field(is2:ie2,js2:je2) = buffer(pos)
enddo
```

In the above code segment, MPP\_SEND and MPP\_RECV are simply wrapper routines for standard MPI calls MPI\_SEND and MPI\_RECV, and we consider them as equivalent for the purpose of this article. The above code signal each cpu to send the appropriate slab of the array 'field' to its west neighbor, which then placed this slab into its proper destination. Similar types of communication exist in practically all parallel programs. An important observation to be noted here is that the communication routines are linear operators, hence as matrices, the adjoint is simply the transpose, which is the dual operator. In the code above, we see an efficient characterization of the relationships between domain, cpu, communication task to be performed, and array indices, in their respective order as a chain of pointers.

Once this chain of relationships is established, adjoining the code is relatively simple.

```

do m=1,ncpus
if( recv_e .AND. domain%list(m)%recv_e%overlap )then
is1 = domain%list(m)%recv_e%is1; ie1 = domain%list(m)%recv_e%ie1
js1 = domain%list(m)%recv_e%js1; je1 = domain%list(m)%recv_e%je1
...
buffer(pos) = field(is1:ie1,js1:je1) field(is1:ie1,js1:je1) = 0. ...
endif
call mpp_send( buffer(pos), plen=msgsize, to_pe=to_pe )
if( send_w .AND. domain%list(m)%send_w%overlap )then
is2 = domain%list(m)%send_w%is2; ie2 = domain%list(m)%send_w%ie2
js2 = domain%list(m)%send_w%js2; je2 = domain%list(m)%send_w%je2
endif
call mpp_recv( buffer(pos), glen=msgsize, from_pe=from_pe )
field(is2:ie2,js2:je2) = field(is2:ie2,js2:je2) + buffer(pos)
enddo

```

Now the duality between MPP\_SEND and MPP\_RECV calls is now apparent. In the adjoint code, we send where we received before, and received where we send previously. Similar duality exists for other MPI routines, for example, MPI\_GATHER and MPI\_SCATTER, hence construction of their adjoints can be done in a similar manner.

### 3. CONCLUSIONS

Adjoining a complicated piece of code is normally a tedious task, especially if done manually. Recent developments in automatic differentiation tools have aided greatly in reducing the coding time. However, as of the moment, there are still some major shortcomings with regards to the adjoining of parallel codes. We have shown

that with the proper coding structure and setup, such a task can be done with ease and may be incorporated into future versions of automatic code transformation programs by taking advantage of the natural duality that exists between parallel communication routines.

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